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The synthesis, crystal chemistry and structures of Y-doped brannerite $(U_{1-x}Y_xTi_2O_6)$ and thorutite $(Th_{1-x}Y_xTi_2O_{6-\delta})$ phases

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Abstract

Yttrium-doped uranium brannerite $(U_{1-x}Y_xTi_2O_6)$ and thorutite $(Th_{1-x}Y_xTi_2O_{6-\delta})$ phases were synthesized in air at 1400° C. Powder X-ray diffraction revealed that these phases crystallized to form monoclinic (C2/m) structures. Crystal structures of $U_{0.54}Y_{0.46}Ti_2O_6$ (1) $(a=9.8008(2); b=3.7276(1); c=6.8745(1); \beta=118.38(1); V=220.97(1); Z=2; R_P=7.3\%; R_B=4.6\%)$ and $Th_{0.91}Y_{0.09}Ti_2O_{6-\delta}$ (2) $(a=9.8002(7); b=3.7510(3); c=6.9990(5); \beta=118.37(4); V=226.40(3); Z=2; R_P=4.5\%; R_B=2.9\%)$ were refined from powder neutron diffraction data. These two phases were isostructural, revealing planes of corner and edge-sharing TiO_6 octahedra separated by irregular eight-fold coordinate U/Y or Th/Y atoms. The oxygen sites within the structure of 1 were found to be fully occupied, confirming that the doping of lower valence Y atoms occurs in conjunction with the oxidation of U(IV) to U(V). Y doping of the thorutite phase 2 does not lead to oxidation but rather the formation of oxygen vacancies within the structure.

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1. Introduction

Brannerite, UTi₂O₆, has been found to be present as a minor phase in titanate-based pyrochlore-rich ceramics of the synroc [1] type designed for the geological immobilization of excess weapons Pu [2,3]. Brannerite in these ceramics was found to incorporate neutron absorbers such as Gd and Hf as well as Pu and U. The neutron absorbers are present in these ceramics to overcome potential criticality problems associated with the presence of Pu.

Natural brannerite occurs as a mineral that is nearly always X-ray amorphous because of radiation damage from α -decay of U, Th and daughter isotopes. Crystalline forms of brannerite having a monoclinic structure have been produced either by recrystallization at $\sim 1000^{\circ}$ C [4,5] or by synthesis under low-oxygen conditions [4]. Furthermore, it has recently been shown that incorporation of other divalent, trivalent and tetravalent dopants provides a means of stabilising brannerite phases produced in air [6,7].

*Corresponding author. Fax: +61-2-9717-3606. E-mail address: mja@ansto.gov.au (M. James). The present work examines the substitutional chemistry of brannerite (UTi₂O₆) and thorutite (ThTi₂O₆) phases as a function of yttrium doping to form U/Th_{1-x}Y_xTi₂O₆. We report structural changes as a function of Y-content and in particular describe the structures of U_{0.54}Y_{0.46}Ti₂O₆ (1) and Th_{0.91}Y_{0.09}Ti₂O_{6- δ} (2) as determined by powder neutron diffraction.

2. Experimental

2.1. Synthesis

The samples were prepared by the alkoxide/nitrate route [8]; the mixtures dried and calcined in air at 750°C for 1 h. The calcines were wet milled for 16 h and dried before cold pressing and firing the pellets for 14 h at 1400°C under air.

2.2. Electron microscopy

Scanning electron microscopy (SEM) was carried out with a JEOL 6400 instrument run at 15 kV, and fitted with a Tracor Northern TN5502 energy-dispersive

X-ray (EDX) detector, which utilized a comprehensive set of standards for quantitative work.

2.3. Diffraction measurements

Powder X-ray diffraction measurements were made on a Scintag Inc. XGEN 4000 X-ray diffractometer at ambient temperature using $CuK\alpha$ radiation and a flat-plate sample holder. Data of sufficient quality for structural refinement were collected over $5^{\circ} < 2\Theta < 85^{\circ}$, in 0.025° steps, with integration times of 10 s. Powder neutron diffraction measurements were also made on the high-resolution powder diffractometer (HRPD) using thermal neutrons ($\lambda = 1.4930 \,\text{Å}$ (1), 1.8855 Å (2)) from the HIFAR nuclear reactor at ANSTO [9]. Data was collected using a bank of 24 3 He detectors over the range $10^{\circ} < 2\Theta < 140^{\circ}$, in 0.05° steps, with the measurement of 1 taking 44 h and 2 taking 32 h. Structural refinements were carried out by the Rietveld method [10] using the RIETICA program [11], with pseudo-Voigt peak shapes and refined backgrounds. Further details of the crystal structure investigation(s) can be obtained from the Fachinformationszentrum Karlsruhe, 76344 Eggenstein-Leopoldshafen, Germany (fax: +49-7247-808-66; mailto: crysdata@fiz-karlsruhe.de) on quoting the depository numbers CSD-412851 for 1 and CSD-412852 for **2**.

3. Results and discussion

3.1. Crystal chemistry and solid solution range

Our previous work indicated that sintering the correct stoichiometry in argon produced single-phase brannerite UTi_2O_6 , however sintering in air produced U_3O_8 and TiO_2 . Brannerite phases were also stabilized in an air atmosphere at high temperatures by substitution of Ca^{2+} or lanthanide ions for U^{4+} with oxidation of the remaining uranium to U^{5+} [6,7].

As was the case for the doped $U_{1-x}M_xTi_2O_6$ phases [7], the solid solution range of $U_{1-x}Y_xTi_2O_6$ depends on the firing atmosphere. Under-doped samples prepared in air gave rise to brannerite phases, U_3O_8 and TiO_2 impurities, while over-doped samples contained brannerite phases, TiO_2 and pyrochlore phases $(Y_{1+x}U_{1-x}Ti_2O_7)$. Over-doped samples of thorutite gave rise to $Th_{0.91}Y_{0.09}Ti_2O_{6-\delta}$ as well as the impurities ThO_2 and Y-rich $Y_2Ti_2O_7$. SEM and EDX analysis were used to characterize the solid solution range for the $U_{1-x}Y_xTi_2O_6$ phases formed at $1400^{\circ}C$. $U_{1-x}Y_xTi_2O_6$ showed a similar solid solution range $(0.29 \le x \le 0.46)$, to other rare earth doped brannerite phases prepared in air $(La^{3+}$: $0.38 \le x \le 0.50$ and Gd^{3+} : $0.31 \le x \le 0.50$),

and a more extensive range than calcium-doped brannerite $(0.21 \le x \le 0.28)$ [7]. It is assumed that no oxygen vacancies are produced in $U_{1-x}Y_xTi_2O_6$ and that U(IV) is oxidized to U(V) in order to compensate for the introduction of Y^{3+} . Thus, sintering of $U_{1-x}Y_xTi_2O_6$ in air gave rise to $\binom{x}{(1-x)}$ U(V) (i.e. between 41% and 87%).

In contrast, the solid solution range for Y-doped $ThTi_2O_6$ was found to be far more restricted than observed for $U_{1-x}Y_xTi_2O_6$ with a lower limit of 0 and an upper limit of only 0.09. With only a $\sim 3\%$ difference in ionic radii between Th^{4+} and Y^{3+} , there is little suggestion that size differences are the major factor in the limited solid solution range. The key lies more with the inability of thorium to be oxidized beyond Th(IV). This is not a surprise given that synthetic or natural compounds having oxidation states of Th(V) or higher have not been previously reported. Thus, the only mechanism of charge balance is via oxygen vacancy formation and unlike brannerite, doping of thorutite by Y^{3+} does not lead to the oxidation of Th(IV) to Th(V).

As was found to be the case for doped brannerite phases $U_{1-x}M_xTi_2O_6$ ($M=Ca^{2+}$, La^{3+} , and Gd^{3+}) [7], other rare earth ions such as Gd^{3+} were also found to substitute for Th^{4+} in $ThTi_2O_6$ at similar levels to that observed for $Th_{0.91}Y_{0.09}Ti_2O_{6-\delta}$. Unlike the doped brannerite materials however, Ca^{2+} was not found to substitute into $ThTi_2O_6$.

4. Structural refinements

4.1. X-ray diffraction profiles

In each case the X-ray diffraction patterns of U_{1-x}Y_xTi₂O₆ could be indexed based on the monoclinic C2/m cell of uranium brannerite UTi₂O₆ [4]. Attempts to refine the structures of these phases using the structure of UTi₂O₆ as an initial model were however unsuccessful, leading to very high residuals $(R_p \sim 20\%)$ or unstable refinements. Comparison of the observed diffraction profiles with those calculated from idealized structures based on UTi₂O₆ indicated strong preferred orientation of the crystallites. Refinement of the Dollase preferred orientation function [12] along different directions did not lead to significant improvements in the fit to the data. Examination of the refined structures revealed significant 'non-physical' distortions, serving to highlight the difficulty in modelling substantial preferred orientation when using flat-plate Bragg-Brentano powder X-ray diffraction data. Unit-cell parameters were however able to be extracted from the powder X-ray diffraction data using the RIETICA program and the Le Bail method [13].

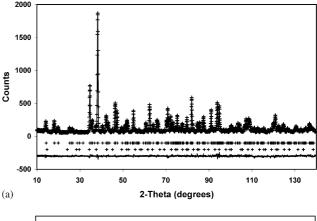
4.2. Neutron diffraction profiles

Due to the difference in scattering geometry, preferred orientation concerns were removed from the structural refinements when powder neutron diffraction data were used. Neutron diffraction data have the additional benefit of providing increased contrast with respect to the oxygen atoms than could be obtained by XRD, particularly given the presence of heavy atoms such as vttrium, thorium and uranium.

The structural parameters for 1 and 2 were determined by Rietveld refinement using the RIETICA program in space group C2/m with Y and U/Th disordered over the 8 coordinate actinide 2a (0,0,0) sites (Table 1). The diffraction profiles for 1 revealed essentially a phase pure sample, although closer examination revealed a small amount of Y/U pyrochlore; this being consistent with the proximity of the sample to the phase boundary. Attempts were made to refine the Y/U ratio, however strong correlations were found to exist between the Y/U site occupancies and the isotropic thermal parameter. Therefore, the site occupancies of Y and U were set at their composition as determined by EDX (0.46 and 0.54, respectively). In the final stages of the refinement the occupancy of the oxygen sites of 1 were refined and were found to be fully occupied; this being consistent with the oxidation of U(IV) to U(V) and no formation of oxygen vacancies. The pyrochlore impurity was included as a second phase in the structural model, leading to a noticeable improvement in the quality of the refinement $(R_p \sim 5.9\% \rightarrow R_p \sim 4.9\%)$. The refined molar fraction of pyrochlore was determined as 2.1(1)%. The observed, calculated and difference diffraction profiles for 1 and 2 are shown in Figs. 1(a) and (b), respectively.

Table 1 contains crystallographic information extracted from powder diffraction data for end-member compositions of $U_{1-x}Y_xTi_2O_6$ and **2**. Examination of Table 1 reveals the effect of doping on the brannerite structure. Replacing U^{4+} having an ionic radius of $1.00\,\text{Å}$ [14], by the slightly larger Y^{3+} ion $(1.019\,\text{Å})$ in $U_{0.54}Y_{0.46}Ti_2O_6$ is off-set by the oxidation of the remaining uranium to the smaller $(0.89\,\text{Å})$ U^{5+} . The doping and subsequent oxidation leads to a contraction in the unit cell from $224.1(1)\,\text{Å}^3$ as present in UTi_2O_6 (1) to $219.12(1)\,\text{Å}^3$ in $U_{0.54}Y_{0.46}Ti_2O_6$. Refined atomic positions and thermal parameters are given in Table 2 and the refined structure (of **1**) is displayed in Fig. 2. Selected bond lengths are displayed in Table 3.

As has been observed in numerous perovskite-based compounds, significant variation in ionic size or charge can lead to ordering of the individual ionic species onto distinct crystallographic sites along with an accompany-



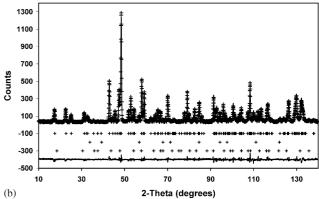


Fig. 1. The observed (crosses), calculated and difference (solid lines) powder neutron diffraction profiles for (a) $U_{0.54}Y_{0.46}Ti_2O_6$ (1) and (b) $Th_{0.91}Y_{0.09}Ti_2O_{6-\delta}$ (2).

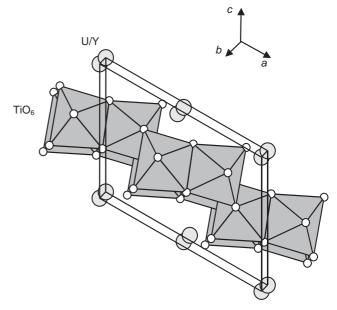


Fig. 2. The refined crystal structure of $U_{0.54}Y_{0.46}T_{i_2}O_6$ (1), showing sheets of corner and edge-sharing TiO_6 octahedra along the *ab* plane and eight-fold coordinate U/Y atoms between the planes.

ing change in unit-cell dimensions (i.e., the formation of a super-lattice structure). Careful examination of the neutron and X-ray diffraction profiles of both did not

Table 1 Crystallographic data for $U_{0.71}Y_{0.29}Ti_2O_6$, $U_{0.54}Y_{0.46}Ti_2O_6$ (1) and $Th_{0.91}Y_{0.09}Ti_2O_{6-\delta}$ (2)

Formula	U _{0.71} Y _{0.29} Ti ₂ O ₆	U _{0.54} Y _{0.46} Ti ₂ O ₆	$Th_{0.91}Y_{0.09}Ti_2O_{6-\delta}$
Formula weight	386.543	355.227	409.485
Color	Black	Black	Black
$U^{4+}:U^{5+}$ (%)	59:41	13:87	
Space group	C2/m (No. 12)	C2/m	C2/m
Z	2	2	2
a (Å)	9.818(2) ^a	9.8039(2) ^b	9.8176(2) ^b
b (Å)	$3.731(1)^{a}$	3.7188(1) ^b	$3.8141(1)^{b}$
c (Å)	6.876(2) ^a	6.8403(2) ^b	6.8271(3) ^b
β (deg)	118.68(1) ^a	118.52(1) ^b	118.74(1) ^b
$V(\mathring{A}^3)$	221.0(1) ^a	219.12(1) ^b	230.47(1) ^b
$\rho_{\rm calc}~({\rm gcm}^{-3})$	5.809 ^a	5.382 ^b	5.899 ^b
2θ range (deg)	5-85 ^a	10-140 ^b	10-140 ^b
λ(Å)	1.5406 ^a	1.4930 ^b	1.8855 ^b
No. of reflns	98 ^a	279 ^b	148 ^b
$R_{ m P}/R_{ m B}$		$4.9\%/2.2\%^{b}$	$6.6\%/3.0\%^{b}$

^aAs determined from powder X-ray diffraction data using the Le Bail method [14].

Table 2 Fractional atomic coordinates and equivalent isotropic thermal parameters (B_{eq}) (Å $^2 \times 100$) for $U_{0.54}Y_{0.46}Ti_2O_6$ and $Th_{0.91}Y_{0.09}$ $Ti_2O_{6-\delta}$ with Esd's in parentheses, as determined from powder neutron diffraction data

	$U_{0.54}Y_{0.46}Ti_2O_6$	$Th_{0.91}Y_{0.09}Ti_2O_{6-\delta}$
Y/U/Th (2a)		
x	0	0
y	0	0
Z	0	0
$B_{ m eq}$	1.0(1)	1.5(1)
Occ (Y)	0.46	0.09
Occ (U/Th)	0.54	0.91
Ti (4i)		
X	0.8261(4)	0.8265(4)
y	0	0
Z	0.3922(6)	0.3980(4)
$B_{ m eq}$	0.6(1)	0.5(1)
O1 (4i)		
x	0.9785(2)	0.9782(2)
y	0	0
Z	0.3061(3)	0.3140(4)
$B_{ m eq}$	0.9(1)	0.7(1)
O2 (4i)		
x	0.6509(2)	0.6563(3)
y	0	0
z	0.1034(3)	0.1109(4)
$B_{ m eq}$	1.1(1)	0.8(1)
O3 (4i)		
x	0.2835(2)	0.2820(2)
у	0	0
Z	0.4072(3)	0.4083(3)
$B_{ m eq}$	1.1(1)	0.9(1)

provide any evidence for cation ordering in these phases, despite the substantial charge difference between Y^{3+} and U^{5+} and the ($\sim 15\%$) difference in their ionic radii.

The structure of 2 was also refined in a similar fashion from powder neutron diffraction data and was found to be essentially isostructural with 1 with Y and Th disordered over the 2a sites. As was the case of 1 strong correlations prevented refinement of the Y/Th site occupancies. The oxygen site occupancies were also refined and were not found to differ significantly from unity (i.e., they appear to be fully occupied). This result although appearing contrary to the notion of oxygen vacancies, is not unexpected. Given the amounts of Y³⁺ and Th⁴⁺ (as determined by SEM) the oxygen vacancy level is expected to be $\delta \sim 0.045$. With three oxygen sites in the structure, the occupancies with an average vacancy level would only be 0.993. This small vacancy level is beyond the capability to be detected by Rietveld refinement based on neutron diffraction data. In addition to the main phase, small amounts of ThO₂ (3.7%) and Y₂Ti₂O₇ (1.6%) were observed to be present. The refined cell dimensions of 2 (Table 1) were found to be slightly smaller $(V = 230.47(1) \text{ Å}^3)$ than those for ThTi₂O₆ $(V = 231.12(1) \text{ Å}^3)$ [15]. This is reasonable given that eight-fold coordinate Y³⁺ (1.019 Å) is slightly smaller than eight-fold coordinate Th^{4+} (1.05 Å).

The structures of both $U_{0.54}Y_{0.46}Ti_2O_6$ and $Th_{0.91}Y_{0.09}Ti_2O_{6-\delta}$ consist of sheets of corner and edge sharing, TiO₆ octahedra in the ab plane (Fig. 2). The U/Th/Y atoms adopt an irregular eight-fold coordination between these sheets. The average Ti-O bond lengths in 1 (1.956(2) Å) and 2 (1.963(3) Å) are slightly shorter than those typically observed by Shannon (2.005 Å) for other oxides of Ti(IV) [14]. In addition, within each TiO₆ octahedron there is significant variation of Ti-O bond lengths (Table 3), reflecting an irregular coordination. In 1, where octahedra share a common edge, the average distance between adjacent oxygen atoms is 2.49 A, while the average distance between corner-sharing oxygen atoms is substantially longer at 2.90 A. The average observed U-O bond length for 1 (2.396 Å) appears slightly longer than expected from other uranium containing oxides (2.36 A) [14]. It is however an artifact of the highly asymmetric coordination sphere. Examination of Table 3 and Fig. 2 reveals three distinct types of U/Y-O bonds: a pair of short U/Y-O1 bonds (2.203(2)Å), four short bonds (2.269(1) Å) to O2 atoms that bridge pairs of U/Y atoms along the b-axis and a pair of long U/Y-O3 bonds (2.844 Å). By way of comparison, the equivalent bond lengths in UTi₂O₆ were found to be 2.252, 2.296 and 2.824 Å for U-O1, U-O2 and U-O3, respectively [4]. The underlying asymmetric nature of the U/Y coordination sphere in each of these cases is therefore not a

^bAs determined from powder neutron diffraction data using the Rietveld method [11].

Table 3 Selected bond lengths (Å) for $U_{0.54}Y_{0.46}Ti_2O_6$ and $Th_{0.91}Y_{0.09}Ti_2O_{6-\delta}$ as determined from powder neutron diffraction data

	$U_{0.54}Y_{0.46}Ti_2O_6\\$	$Th_{0.91}Y_{0.09}Ti_2O_{6-\delta}$	
U/Th-O1 (×2)	2.203(2)	2.314(2)	
$U/Th-O2 (\times 4)$	2.269(1)	2.334(2)	
$U/Th-O3 (\times 2)$	2.844(2)	2.872(2)	
Ti-O1	1.849(2)	1.847(5)	
Ti-O1	2.038(3)	2.010(3)	
Ti-O2	1.901(3)	1.901(2)	
Ti-O3	2.108(2)	2.092(3)	
Ti-O3 (×2)	1.919(1)	1.965(1)	

consequence of Y-doping. Asymmetric Y–O bond lengths have however also been observed in other eight-fold coordinate titanates such as $Y_2Ti_2O_7$, with two short bonds (2.186 Å) and six long bonds (2.510 Å) [16]. Similar behavior is observed for **2** with a range of Y/Th–O bond lengths (2.314(2)—2.872(2) Å), however the average observed Y/Th–O bond length for **2** (2.464 Å) is very close to that expected from other thorium based oxides (2.46 Å) [14].

5. Bond valence sums

The valence of a site (i) may be calculated by the following expression:

$$V_i = \sum_j \exp((r_0 - r_{ij})/B),$$

where r_{ij} are the observed bond lengths (Table 3), B = 0.37 and values of r_0 are those of Brown and Altermatt [17], with the exception of that for U^{5+} –O (2.094 Å), which we determined as the average of those for U^{4+} –O and U^{6+} –O. Bond valence values were calculated based on the quantities of Y^{3+} , U^{4+} , U^{5+} and T^{4+} as listed in Table 1, giving 4.0(1) for the $Y^{3+}/U^{4+}/U^{5+}$ sites of 1 and 4.1(1) for the Y^{3+}/T^{4+} sites of 2, respectively. Calculation of the Ti valence using the observed Ti–O bond lengths (Table 3) gave 4.2(1) and 4.1(1) for 1 and 2 respectively. In all cases the bond valence calculations for the different sites shows very good agreement with the expected site valences, despite the large amount of structural asymmetry observed for both the U(Th)/Y and Ti sites.

6. Conclusions

We have synthesized Y-doped uranium brannerite and thorutite phases $U_{1-x}Y_xTi_2O_6$ and $Th_{1-x}Y_xTi_2O_{6-\delta}$ at 1400°C in air. The range of solid solution of the former (0.29 < 0.46) was found to be similar to that observed for other rare earth doped brannerites; while yttrium-doped thorutite was found to have only a limited range (up to x = 0.09). Each of the phases produced was found to form a monoclinic structure. Rietveld refinement of powder neutron diffraction data for $U_{0.54}Y_{0.46}Ti_2O_6$ (1) confirms that doping of lower valence Y³⁺ atoms into brannerite occurs in conjunction with the oxidation of U(IV) to U(V). Although not directly observed from the structural refinements in the case of $Th_{0.91}Y_{0.09}Ti_2O_{6-\delta}$ (2), we propose that a small number of oxygen vacancies ($\delta \sim 0.045$) were produced and thorium was not oxidized beyond Th(IV).

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